

## Course Specifications

| Course Title: | NUMBER THEORY |
| :--- | :--- |
| Course Code: | MATH 3270 |
| Program: | BACHELOR OF SCIENCE IN MATHEMATICS |
| Department: | MATHEMATICS |
| College: | COLLEGE OF SCIENCE AND HUMANITIES ALKHARJ |
| Institution: | PRINCE SATTAM BIN ABDULAZIZ UNIVERSITY |

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## A. Course Identification

| 1. Credit hours: $4(4,0,0)$ |  |
| :---: | :---: |
| 2. Course type <br> a. <br> University $\square$ <br> b. | Others $\square$ |
| 3. Level/year at which this course is offered: LEVEL: Elective |  |
| 4. Pre-requisites for this course (if any): Math 2240 |  |
| 5. Co-requisites for this course (if any): Nil |  |

6. Mode of Instruction (mark all that apply)

| No | Mode of Instruction | Contact Hours | Percentage |
| :---: | :---: | :---: | :---: |
| 1 | Traditional classroom | Weekly 5 hours | \%100 |
| 2 | Blended |  |  |
| 3 | E-learning |  |  |
| 4 | Distance learning |  |  |
| 5 | Other |  |  |

7. Contact Hours (based on academic semester)

| No | Activity | Contact Hours |
| :---: | :---: | :---: |
| 1 | Lecture | 48 |
| 2 | Laboratory/Studio | 0 |
| 3 | Tutorial | 0 |
| 4 | Others (specify) - Office Hours | 60 |
|  | Total | 108 |

## B. Course Objectives and Learning Outcomes

## 1. Course Description

Divisibility - Greatest Common Divisor - Division Algorithm - Prime Factorization and Binomial - Binomial Theorem and Congruencies - Congruencies - Residue Systems Fermat's Little Theorem - Euler's Theorem - Wilson's Theorem - Diophantine Equations Chinese Remainder Theorem - RSA Cryptography - Solving Equations Modulo Primes Quadratic Residue Symbol - Quadratic Reciprocity - Continued Fractions -Arithmetic Functions- Introduction to Torsion points and Elliptic Curves.

## 2. Course Main Objective

To make the students familiar with different types of numbers such as prime, composite, pseudo-primes etc., and help the students acquire skill to perform mathematical calculations using modulo arithmetic and their elementary applications.

## 3. Course Learning Outcomes

| CLOs |  | Aligned PLOs |
| :---: | :---: | :---: |
| 1 | Knowledge and Understanding |  |
| 1.1 | Be familiar with the different types of numbers such as prime numbers, composite numbers and associated theorems | K1 |
| 1.2 | Able to recall division algorithm and congruence | K4 |
| 1.3 | Learn and reproduce some elementary theorems such as fundamental theorem of arithmetic, Chinese reminder theorem, Euler's theorem, Fermat's theorem | K2 |
| 2 | Skills : |  |
| 2.1 | Able to check whether a given number is prime or composite using division algorithm | S2 |
| 2.2 | Solve congruence system using Chinese reminder theorem | S2 |
| 2.3 | Able to find continued fractions | S3 |

C. Course Content

| No | List of Topics | Contact Hours |
| :---: | :---: | :---: |
| 1 | Divisibility, Greatest Common Divisor, Division Algorithm, Prime factorization | 6 |
| 2 | Binomial Theorem, Congruencies, residue system | 4 |
| 3 | Fermat's Little Theorem, Euler's Theorem, Wilsons Theorem | 6 |
| 4 | Linear Diophantine Equations | 4 |
| 5 | Chinese Reminder Theorem | 6 |
| 6 | RSA Cryptography | 3 |
| 7 | Solving Equations using modulo primes | 6 |
| 8 | Quadratic Residue Symbol | 3 |
| 9 | Continued Fractions | 3 |
| 10 | Arithmetic Functions | 4 |
| 11 | Torsion Points and Elliptic Curves | 3 |
|  | Total | 48 |

## D. Teaching and Assessment

1. Alignment of Course Learning Outcomes with Teaching Strategies and Assessment Methods

| Code | Course Learning Outcomes | Teaching Strategies | Assessment Methods |  |
| :---: | :---: | :---: | :---: | :---: |
| 1.0 | Knowledge and Understanding |  |  |  |
| 1.1 | Be familiar with the different types of numbers such as prime numbers, composite numbers and associated theorems | 1.E-learning <br> 2.Interactive sessions <br> 3.Exclusive Office Hours for clearing doubts in small groups | 1. Two Internal  <br> Exams   <br> 2. At least two  <br> Quiz   <br> 3. End Semester <br> Exam   |  |
| 1.2 | Able to recall division algorithm and congruence |  |  |  |
| 1.3 | Learn and reproduce some elementary theorems such as fundamental theorem of arithmetic, Chinese reminder theorem, Euler's theorem, Fermat's theorem |  |  |  |
| 2.0 | Skills |  |  |  |
| 2.1 | Able to check whether a given number is prime or composite using division algorithm | 1. Application oriented exercises during tutorial session. <br> 2. Homework to improve the analytical skills | $\begin{aligned} & 1 . \\ & 2 . \\ & 3 . \end{aligned}$ | Homework Assignments Quiz |
| 2.2 | Solve congruence system using Chinese reminder theorem |  |  |  |
| 2.3 | Able to find continued fractions |  |  |  |

2. Assessment Tasks for Students

| \# | Assessment task* | Week Due | Percentage of Total Assessment Score |
| :---: | :---: | :---: | :---: |
| 1 | Mid Term Exam I | 6 | 20\% |
| 2 | Quiz | 4 \& 10 | 5\% |
| 3 | Mid Term Exam II | 13 | 20\% |
| 4 | Continuous Assessment - Homework, Assignment, Attendance etc. | -- | 5\% |
| 5 | End Semester Exam | 15 | 50\% |



## E. Student Academic Counseling and Support

Arrangements for availability of faculty and teaching staff for individual student consultations and academic advice :

Exclusive office hours - 5 hours a week
Academic advising -1 hour per week

## F. Learning Resources and Facilities

## 1.Learning Resources

| Required Textbooks | 1-Niven Ivan, Herbert S. Zuckerman and Hugh L. Montgomery, "An <br> Introduction to the Theory of Numbers". New York: Wiley Text <br> Books, ISBN: 0471625469. <br> 2-Introduction to Modern Number Theory, Fundamental Problems, <br>  <br> Ideas and Theories, Yuri Ivanovic Manin. <br> 3- Number Theory for Mathematical Contests, David A. <br> SANTOS |
| :--- | :--- |


|  |  |
| :---: | :---: |
| Essential References <br> Materials | NIL |
| Electronic Materials | Introductory Number Theory - M Stoll |
| Other Learning <br> Materials | Lecture Notes Prepared by the Department of Mathematics |

## 2. Facilities Required

| Item | Resources |
| :---: | :---: |
| Accommodation <br> (Classrooms, laboratories, demonstration <br> rooms/labs, etc.) | 1. Classrooms with Smart boards with seating <br> facilities for at least 30 students |
| Technology Resource <br> (AV, data show, Smart Board, software, | Smartboard, Internet Connection for Blackboard |
| Other Resources <br> (Specify, e.g. if specific laboratory <br> equipment is required, list requirements or <br> attach a list) |  |

## G. Course Quality Evaluation

| Evaluation Areas/Issues | Evaluators | Evaluation Methods |
| :---: | :---: | :---: |
| Effectiveness of Teaching | Students, Graduates | Course Evaluation and <br> Program   <br> (Indirect)   |
|  | Program Leaders | Peer Review (Direct) |
| Achievement of CLOs | Faculty and Quality Personnel | Direct (Tests and Quiz) and Review of Course Report |
| Quality of LearningResources | Students | Course Evaluation (Indirect) |
|  | Graduates | Program Evaluation(Indirect) |
| Facilities | Students / Graduates | Course and <br> Evaluation (Indirect)  |
|  | Faculty | Faculty Survey (Indirect), Course Reports (Direct) |

Evaluation areas (e.g., Effectiveness of teaching and assessment, Extent of achievement of course learning outcomes, Quality of learning resources, etc.)
Evaluators (Students, Faculty, Program Leaders, Peer Reviewer, Others (specify)
Assessment Methods (Direct, Indirect)
H. Specification Approval Data

| Council / Committee |  |
| :---: | :---: |
| Reference No. |  |
| Date |  |

